Test Suite Generation of t-way CIT with constraints for Web Based Application

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Abstract - Web based applications are increasing in importance as consumers use web for wide range of daily activities. Testing the web based applications as banking with large number of interactions is crucial. Combinatorial Interaction testing is a method that generates test suites incrementally using combinatorial explosion strategy for testing. There are some unknown combinations that are impossible to occur due to the constraints in the application termed as constraints. There arise practical problems when adding constraints between combinations of input domain resulting in combinatorial explosion. This paper presents a new algorithm that features the construction of test suites to support combinatorial interaction testing.

Keywords - Interaction testing, Combinatorial Testing, Constraints, Test suite generation

I. INTRODUCTION

A combinatorial testing approach is a kind of functional testing technique consisting of exhaustively validating all combinations of size t of applications input values. It requires formal modeling of application features as input values. Modeling activities are expensive and time consuming. The tester models only the inputs and requires that they are sufficiently covered by tests. On the other hand unintended interactions between the input parameters can lead to incorrect behavior which may not be detected by traditional testing. In particular Combinatorial Interaction Testing aims at generating the reduced-size test suite which covers all combination of input values with constraint support. Predicates and constrained covering array is used to generate test suites which forms the basis for combinatorial interaction testing.

II. COVERING ARRAYS

A t-way CIT sample is a mathematical structure called covering array [1,2]. From the mathematical point of view, the problem of generating a minimal set of test suites covering all combinations of input values is equivalent to finding a covering array of strength t over a heterogeneous interaction. Covering arrays [3] are combinatorial structures which extend the notion of orthogonal arrays.

DEFINITION 1. An instance called an orthogonal array, OA(t, k, v) where every ordered subset occurs exactly once. In this case N is not used because the exact size of the array is always v^t.

OAs are tabular arrangement of symbols which satisfy certain combinatorial properties. It is the generalization of latin squares [4]. If OA Strength = 2 then every 2 columns contains all possible pairs of elements. Often OA matching the required combinatorial test structures does not exist. OAs don’t support constraint among test settings and parameters.

DEFINITION 2. A covering array, CA(N; t, k, v), is an N × k array on v symbols with the property that every N × t sub-array contains all ordered subsets of size t from the v symbols at least once.

An N × k array with the property that in every N × t sub-array, each t-tuple occurs at least \( \lambda \) times, where t is the strength of the coverage of interactions, k is the number of parameters (degree), and \( g = (g_1; g_2; \ldots g_k) \) is a vector of positive integers defining the number of values for each parameter.

DEFINITION 3. A mixed level covering array, MCA(N; t, k, (v_1, v_2, ..., v_k)), is an N × k array on v symbols, where v = \( P_k i=1 v_i \), with the following properties:

1. Each column i (1 \( \leq \) i \( \leq \) k) contains only elements from a set \( S_i \) of size \( v_i \).
2. The rows of each N × t sub-array cover all t-tuples of values from the t columns at least 1 time.

A shorthand notation is used to describe mixed level covering arrays [5] by combining equal entries in \( (v_i : i \leq 1 \leq k) \). For example three entries each equal to 2 can be written as 2^3.

III. CONSTRAINED COVERING ARRAYS

The presence of constraints demands new definition of proper CIT sample. Integral to this concept is whether t-set is consistent with constraints [6].

DEFINITION 4. Given a set of constraints C, a given t-set, s, is C-consistent if s is not forbidden by any combination of constraints in C.

This definition permits flexibility in defining the nature of constraints and how they combine to forbid combinations.

DEFINITION 5. A constrained-covering array, denoted CCA(N; t, k, v, C), is an N × k array on v symbols with constraints C, such that every N × t sub-array contains all ordered C-consistent subsets of size t from the v symbols at least once. We extend this definition to constrained mixed-level covering arrays CMCA(N; t, k, (v_1, v_2, ..., v_k), C) in the natural way.
A desired requirement of combinatorial interaction testing strategy is the ability to deal with complex constraints [7,8]. Although the presence of constraints reduces the size of combinatorial test suites it also makes test generation more challenging. The general problem of finding minimal test suite that satisfies t-wise interaction coverage is NP complete. If constraints are added on the input domain finding a single test suite that satisfies t-wise interaction coverage is NP complete.

There are already a few approaches dealing with constraints over the input domain [9, 10]. In order to deal with constraints some methods require remodeling the original specification. Some algorithms simply ignore constraints to post process the test suites, some others delete the combination of input that do not satisfy the constraints. The summary of constraint handling in the existing algorithms/tools is presented in table 1.

### IV. Constraint Support

A desirable requirement of combinatorial interaction testing strategy is the ability to deal with complex constraints [7,8]. Although the presence of constraints reduces the size of combinatorial test suites it also makes test generation more challenging. The general problem of finding minimal test suite that satisfies t-wise interaction coverage is NP complete. If constraints are added on the input domain finding a single test suite that satisfies t-wise interaction coverage is NP complete.

<table>
<thead>
<tr>
<th>Algorithm/Tool</th>
<th>Tool Category</th>
<th>Constraint Handling</th>
<th>Re-Implementable</th>
</tr>
</thead>
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<tr>
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<td>AETG - Like Greedy</td>
<td>REMODEL</td>
<td>PARTIAL</td>
</tr>
<tr>
<td>DDA</td>
<td>AETG - Like Greedy</td>
<td>SIMPLE</td>
<td>YES</td>
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<td>Which:CTS</td>
<td>Construction</td>
<td>EXPAND</td>
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<tr>
<td>Which:TOFU</td>
<td>Unknown</td>
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<tr>
<td>IPO</td>
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<tr>
<td>Constraint Solver</td>
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</tr>
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</table>

### V. Model By Test Predicates

The approach formalizes combinatorial coverage by logic predicates [11, 12]. The preliminary definition of test and test suite is as follows. Given m input parameters, each ranging in its finite domain, a test is an assignment of values to each of the m parameters: p1 = v1, p2 = v2, …, pm = vm where p = v. A test suite is a finite set of tests. The size of the test suite is the number of tests in it. To formalize CIT, express each of the combination of input as logic Tpred expression.

For Example: p1 = v1, p2 = v2, where p1 and p2 are two inputs or monitored variables of enumeration or boolean domain and v1 and v2 are two possible values of p1 and p2 respectively.

Similarly, t-wise coverage can be modeled by a set of test predicates, each of the type:

\[ p1 = v1 \land p2 = v2 \land \ldots \land pt = vt \equiv T_{pred} \]

where p1, p2, … pt are t input parameters and v1, v2, …, vt are their possible values. The t-wise coverage is represented by the set of test predicates that contains every possible combination of the t input variables with their values. Please note that to reach complete t-wise coverage this has to be true for each t-tuple of input parameters of the considered application.

To build complete set of test predicates required for t-wise coverage of a model, employ a combinatorial enumeration algorithm, which simply takes every possible combination of t input variables and it assigns every possible value to them.

### VI. Test Generation

The actual test generation [13] consists of finding a test that covers a given Tpred i.e., a model for it. As long as constraint is not taken into account the Tpred is a conjunction of atom of the form v = x and the model is trivial where simple algorithm is used. In order to support constraints the logical solver tools such as Symbolic Analysis Laboratory can better suit the task. The SAL Framework combines different tools of abstraction, solving and model checkers and used for test generation.

SAL offers a Bounded Model Checkers BMC and Symbolic Model Checkers SMC. A BMC transforms the model checking problem into a constraint satisfaction problem. A SMC uses Binary Decision Diagrams BDD to efficiently represent states, interaction relations and constraints among them.

In order to generate a test that covers a given combinatorial Tpred, SAL is asked to verify a trap property in the model containing monitored variables [14, 15]. The trap property states that Tpred is never true or never(Tpred). It enforces assignment of values falsifying trap property and satisfying Tpred. The proposed approach is able to deal with temporal constraints and able to include state transition and interaction information that cannot be represented by SAT Solvers.

A) IG-t-CCIT

The IG-t-CCIT is the Incremental Generation of t-way test suites with Constrained CIT with Tpred. The basic way to generate suitable test suite for t-wise coverage consist of executing the test predicate generator to generate predicate tree and order the Tpred. Then collect all ordered test predicate from the list of candidate set and execute the SAL to remove the Tpred one by one until candidate set is empty. The SAL generates the test and passes on to Coverage Evaluator. The test plus Coverage information is passed on to test suite generator which works in two stages namely the expansion and contraction or reduction stage and provides the list of test suites.
B) $T_{pred}$ Tree Construction

The Algorithm for the construction of $T_{pred}$ Tree is as given in algorithm 1

**Algorithm 1 : $T_{pred}$ Tree Construction**

**Input :** Monitored Parameters MP, List of Constraints C  
**Output :** Test Predicate Tree $T$

Begin  
Generate list of tuples based on MP and store in CCA  
X = get first tuple from CCA  
Y = get other tuple from CCA  
While X is not complete $T_{pred}$ Tree  
If X and Y can be fused and agree with all constraints C  
Fuse X and Y to form new X  
End if  
Y = get other tuple from CCA  
End While  
Store X in T  
Remove tuples covered by X from CCA  
End

C) Monitoring

Every time a new test $ts$ is added to the test suite, $ts$ always covers as many as $\binom{m}{t}$-wise test predicates, where $m$ is the number of a system's input parameters and $t$ is the strength of the covering array ($t > 2$ for combinatorial interaction testing). Checking which test predicates are covered by $ts$ and remove them from the candidates leads to fewer calls to the model checker and possibly to smaller test suites. To enable monitoring, the tool detects if any additional test predicate $T_{pred}$ in the candidates is covered by $ts$ by checking whether $ts$ is a model of $T_{pred}$ (i.e. it satisfies $T_{pred}$) or not, and in the positive case it removes $T_{pred}$ from the candidates. Checking if a test is a model for a test predicate requires very limited computational effort [16]. This activity is performed by the Coverage Evaluator (stage 5 in Figure 1), which also computes the expected outputs as values for controlled parameters, if any.

D) $T_{pred}$ Ordering

If monitoring is applied, the order in which the candidate test predicates are chosen and processed has a major impact on the size of the final test suite[17, 18]. In fact, each time a $T_{pred}$ is selected, a corresponding test case is generated, covering also other test predicates, which will be then removed from the candidate pool too. In fact, the more the candidate pool is reduced, the less the variety of test cases will be. Considering test predicates in the same order in which they are generated may lead to not optimal test suites. For this reason, insert an additional processing stage (stage 2 of Figure 1) in which the test predicates are ordered according to a user specified policy.

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Figure 1: Test Suite Generation Process by IG-t-CCIT Approach

Figure 2: A Schema of Anti-diagonal indexing of combination values
E) Reduction
Monitoring can significantly reduce the size of a test suite, but a resulting test suite could still contain redundant tests[19, 20]. For Example, the last generated test might also cover several other test predicates $T_{pred'}$. For this reason the analysis of the test suite is useful to further reduce it.

Test suite reduction (also known as test suite minimization) [21] is often applied in the context when one wants to find a subset of the tests that still satisfies given test goals.

VII. ADDING CONSTRAINTS
Addition of constraints over the input is given by expressing them as axioms in the specification. In the bank mortgaging example, the assumption is that the customers have not availed the loan previously then check the type of customer and income and credit rating.

Axiom loan_notavailprev Over Home : (check Type of Customer)
Axiom Type of Cust = employee : (check crediting implies excellent)
Axiom Type of cust = other : (check Income implies repayable)

To express constraint adopt the language of propositional logic with equality. For example the require constraint is translated by an implication. Note that also input domains must be taken into account when checking axioms consistency [22]. Inconsistent axioms must be considered as a fault in the specification and this case must be (possibly automatically) detected and eliminated [23, 24]. Even with consistent axioms, some (but not all) trap properties can be true: there is no test case that can satisfy the test predicate and the constraints. In this case define the test predicate as infeasible.

**DEFINITION 6.** Let $T_{pred}$ a test predicate, M the specification and $C_j$ the conjunction of all the axioms. If the axioms are consistent and the trap property for $T_{pred}$ is true i.e. $M \land C_j \Rightarrow \neg T_{pred}$, then $T_{pred}$ is infeasible. If $T_{pred}$ is the t-wise test predicate $p_1 = v_1 \land p_2 = v_2 \ldots pt=vt$ then this combination of assignments is infeasible.

An infeasible combination of assignments represents a set of invalid test suites which contain such a combination are invalid. The proposed algorithm is able to detect an infeasible assignment since it can actually prove the trap property derived from it. In the bank mortgaging example consider M as loan_availed and $C_j$ as Income $<$ Required the implication that is repayable property becomes false and combination is clearly infeasible. Stated Mathematically $M \land C_j \Rightarrow \neg T_{pred}(Repayable = False)$.

Note that this infeasible combination is not explicitly listed in the constraints. Infeasible combinations represent implicit constraints. So every time we add the test predicate to conjoint of test predicates there is a need to check the consistency by considering the axioms also.

VIII. RESULTS AND DISCUSSION
The proposed approach has been implemented in the ATGT. ATGT allows the tester to load an external file containing the user defined tests and goals [25, 26]. When the external file is loaded ATGT adds the user defined goals to set of test predicates to be covered. Then it adds the user defined tests and checks which $T_{pred}$ are satisfied by these tests. The proposed approach is applied to the web based banking application with different domain sizes using the constrained covering array. The approach is used to benchmark the size of generated test suite and assess the different test generation strategies.

### Table 2: Test Suite Size Comparison using Different Ordering for Unconstrained Models

<table>
<thead>
<tr>
<th>Task</th>
<th>Size</th>
<th>No Collect</th>
<th>Collect</th>
<th>Time (Secs)</th>
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<td>CA5</td>
<td>7</td>
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</table>

### Table 3: Test Suite Size Comparison using Different Ordering for Constrained Models

<table>
<thead>
<tr>
<th>Task</th>
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<th>Collect</th>
<th>Time (Secs)</th>
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</table>
The comparison of the test suite size using unconstrained model and constrained model is given in table 2 and table 3. The results are worthwhile in terms of time and number of test suites. The Result chart shows the time difference for the generation of test suites for the unconstrained and constrained models.

**Figure 3: Test Suite Size and Time for Unconstrained Models**

**Figure 4: Test Suite Size and Time for Constrained Models**

IX. CONCLUSION

This paper presented the approach to t-way combinatorial test suite generation with support of constraints based on the predicates. The IG-t-CCIT has the ability to express complex constraints on the input domain in a compact and effective syntax as formal predicate expressions and axioms and able to generate optimized test suites along with user specific test goals. The constraint handling is done by predicates without having to remodel or expansion. It supports enumerative and Boolean types.

REFERENCES


